

# Perturbative QCD

KONNEVESI RETREAT 2022

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Ilkka Helenius

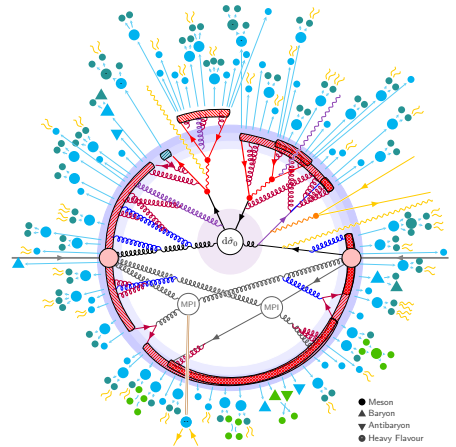
November 17th, 2022



- Hannu Paukkunen
- Ilkka Helenius

## Ongoing research

- Nuclear Parton Distribution Functions and evolution equations
- Heavy-flavour production
- Fragmentation Functions
- Ultra-peripheral collisions
- Pythia Monte-Carlo event generator



[figure by P. Skands]

# Collinear factorization

## Factorize long- and short-distance physics

$$\frac{d\sigma^{AB \rightarrow h+X}}{dp_T \eta} = \int \frac{dz}{z} dx_1 dx_2 f_i^A(x_1, \mu_{\text{fact}}) f_j^B(x_2, \mu_{\text{fact}}) \frac{d\sigma^{ij \rightarrow k+X}}{dp_T \eta} D_k^h(z, \mu_{\text{frag}}) + \mathcal{O}(1/Q^2)$$

- $f_i^A(x, \mu_{\text{fact}})$ : Describe the partonic content of colliding hadron, determined in global analysis applying DGLAP equations
- $\frac{d\sigma^{ij \rightarrow k+X}}{dp_T \eta}$ : Partonic coefficient functions, calculated in perturbative QCD
- $D_k^h(z, \mu_{\text{frag}})$ : Parton-to-hadron fragmentation functions, determined in global analysis applying DGLAP equations

## DGLAP evolution equations for PDFs

$$\frac{\partial f_i(x, Q^2)}{\partial \log(Q^2)} = \frac{\alpha_s(Q^2)}{2\pi} \sum_j \int_x^1 \frac{dz}{z} P_{ij}(z) f_j(x/z, Q^2)$$

# Nuclear parton distribution functions (nPDFs)

## Factorize initial-state nuclear effects

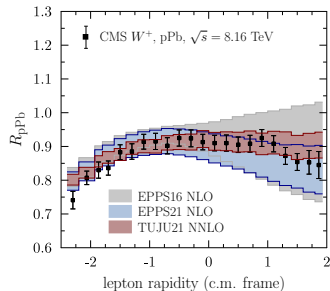
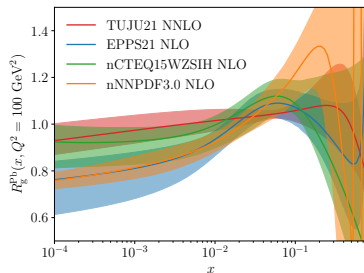
- Parametrize nuclear modification at the initial scale  $Q_0^2 = \mathcal{O}(m_c)$

$$f_i^{p/A}(x, Q_0^2) = R_i^A(x, Q_0^2) f_i(x, Q_0^2)$$

- Fit parameters in  $R_i^A(x, Q_0^2)$  using experimental data

## Contributions to several analyses

- EPPS21 [Eskola, Paakkinen, Paukkunen, Salgado; EPJC 82 (2022) 5, 413]
- TUJU21 [Helenius, Walt, Vogelsang; PRD 105 (2022) 9, 9]
- nCTEQ15 [Duwentäster et. al.; PRD 105 (2022) 11, 114043]

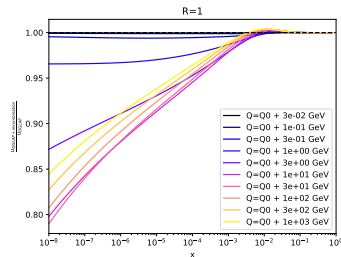
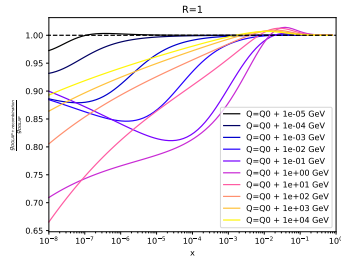


# Non-linear evolution in proton PDFs

## Include recombination effects to DGLAP

[Pit Duwentäster, Vadim Guzey]

- Old GLR does not conserve momentum
- Energy-conserving gluon recombination terms  $P_i^{gg \rightarrow g}$  and  $P_i^{gg \rightarrow q\bar{q}}$  available  
[Zhu and Ruan NPB 559 (1999) 378–392]
- Combine with linear DGLAP terms
- Compare evolution with the linear one for CJ15 proton PDFs
- $R$  parameter related to proton size
- Aim: Global fit including HERA data



## Compare two evolution equations

[Armesto, Lappi, Mäntysaari, Paukkunen, Mirja Tevio;

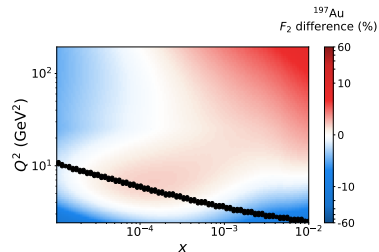
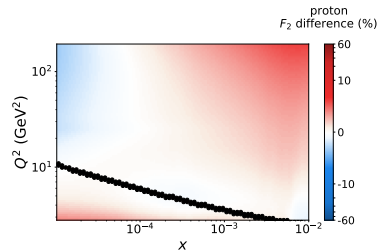
Phys.Rev.D 105 (2022) 11, 114017]

- Match the structure functions  $F_2$  and  $F_L$  at  $x, Q^2$  region where both applicable
- Evolve with DGLAP and BK and see where they differ

$$\text{Relative difference} = \frac{F_2^{\text{BK}} - F_2^{\text{DGLAP Rew}}}{F_2^{\text{BK}}}$$

- Differences pronounced in nuclear case

Ongoing work to study evolution in a physical basis



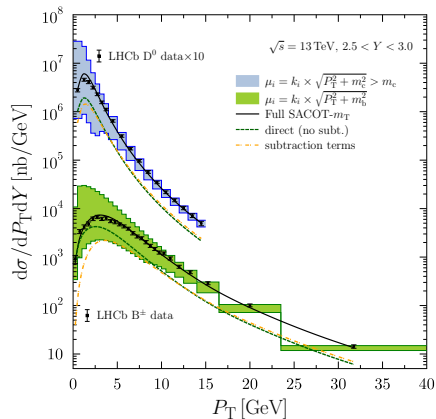
# Heavy-flavour production

## Two well-defined limits

- Fixed-flavour number scheme valid at low  $p_T$
- Massless scheme at high  $p_T$

## Generalized-mass-variable-flavour-number scheme (GMVFNS)

- Combines the regions, applicable at any  $p_T$
- SACOT- $m_T$  scheme with kinematic constraints  
[Helenius, Paukkunen; JHEP 05 (2018) 196]
- Applied also to p+Pb collisions to constrain nPDFs [Eskola, Helenius, Paakinen, Paukkunen; JHEP 05 (2020) 037]
- And to double-heavy flavour production  
[Helenius, Paukkunen; PLB 800 (2020) 135084]



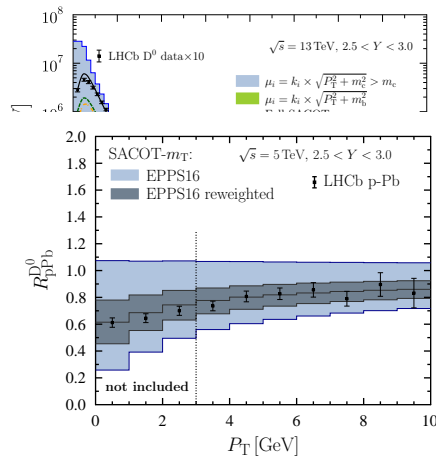
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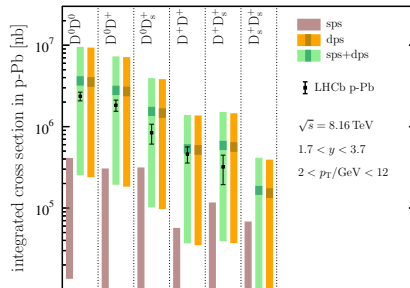
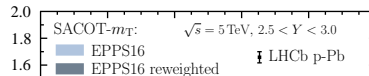
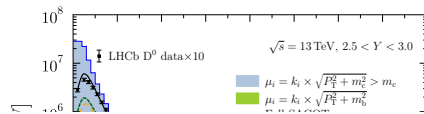
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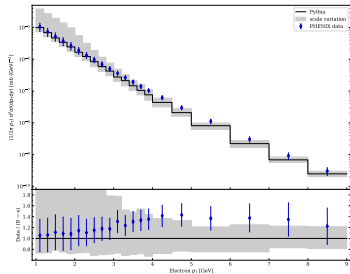
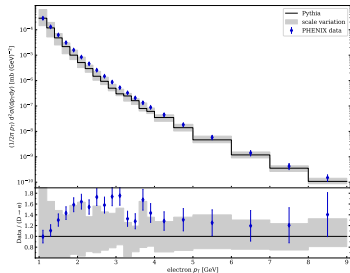
# Heavy-flavour decays

## Leptons from heavy-flavour decays

- Experimentally decay leptons can be identified from displaced vertex
- Theoretically involves convolution of heavy-flavour spectra with “decay function”

## Decays with PYTHIA [Alex Tolvanen, MSc thesis]

- Sample heavy-meson kinematics from SACOT- $m_T$  cross section
- Feed particle to PYTHIA to select decay channel and sample kinematics
- Pick decay leptons and form differential cross section



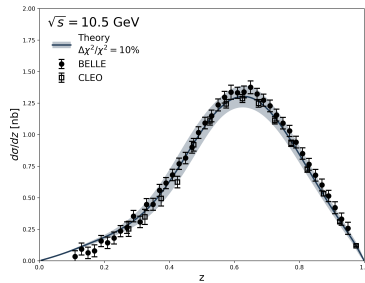
# Heavy-meson fragmentation functions (FFs)

- Similarly as PDFs, also FFs require non-perturbative input to be fitted to data
- Only few works for heavy-flavour FFs, we have applied KKKS08

## New heavy-flavour FF analysis

[Manuel Epele]

- Apply LEP, BELLE and other  $e^+e^-$  data
- Carefully address radiative corrections
- Hessian error analysis to quantify the uncertainty propagation



- Good description of the applied  $D^{\pm*}$  data

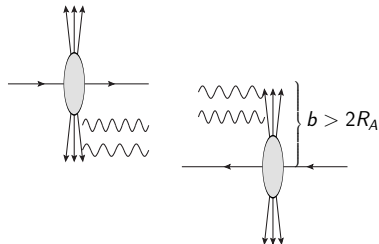
# Ultra-peripheral collisions (UPCs)

- Collisions with large impact parameter  
⇒ No hadronic interactions
- Photons emitted by the charged beam particle may interact

## Equivalent photon approximation (EPA)

[Sami Yrjänheikki, MSc thesis]

- Allows to factorize photon flux from the hard-process cross section
- Applied to exclusive dilepton production in  $p+p$
- Comparison with (different) EPA and full calculation



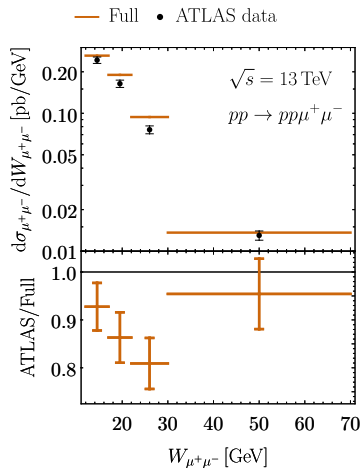
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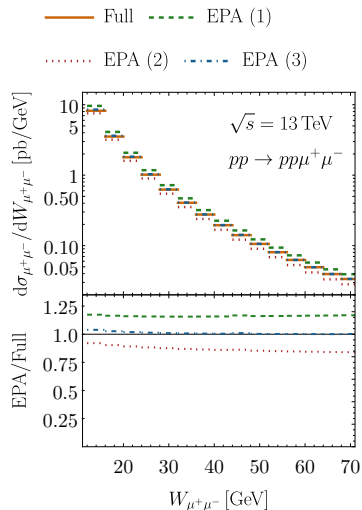
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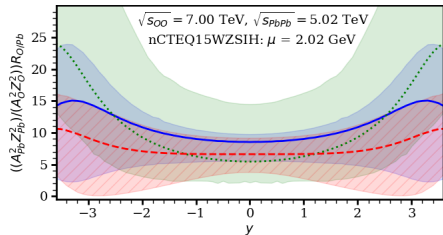
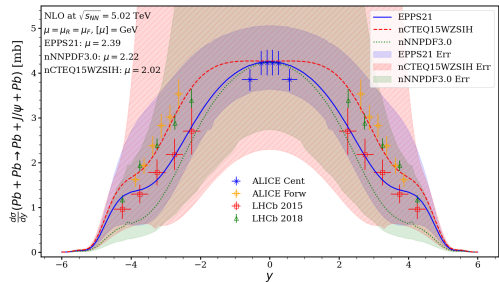
# Exclusive heavy-meson production

## NLO calculation for $J/\psi$ production in ultra-peripheral Pb+Pb collisions

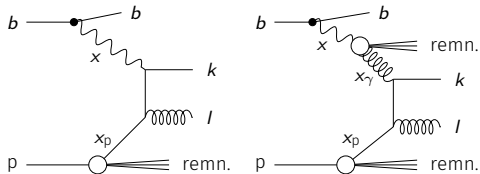
[Eskola, Flett, Guzey, Löytäinen, Paukkunen;  
PRC 106 (2022) 3, 035202]

- First pQCD-based calculation at NLO for exclusive  $J/\psi$  in UPCs
- Sensitive to nPDFs at small- $x$
- Large scale uncertainty
- Applied also to O+O, ratio to reduce the scale uncertainty

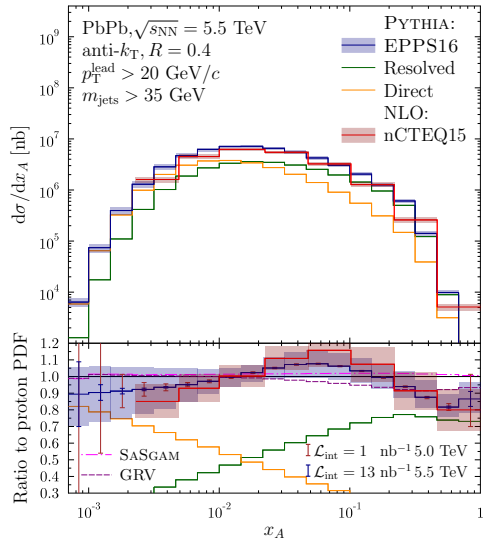
[Eskola, Flett, Guzey, Löytäinen, Paukkunen; arXiv:2210.16048 [hep-ph]]



# Inclusive dijet production in UPCs



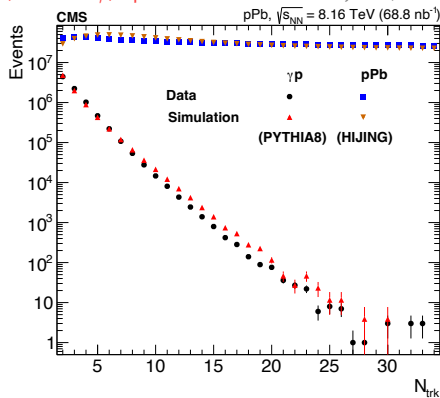
- Another novel process potentially sensitive to nuclear PDFs
- Small- $x$  reach more limited than with  $J/\psi$  but theoretically cleaner
- Exact potential to be quantified [Paakkinen, Guzey]
- NLO and LO Pythia in agreement





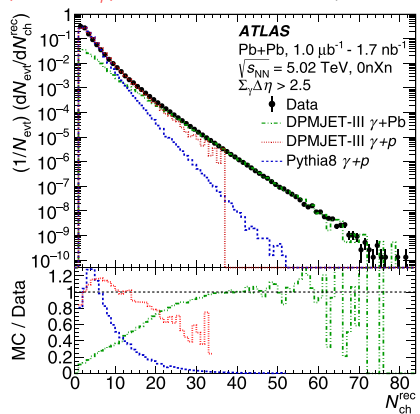
# Ultra-peripheral heavy-ion collisions with PYTHIA

$(\text{Pb} \rightarrow \gamma)+p$ : [CMS: Murillo Quijada, QM2022]

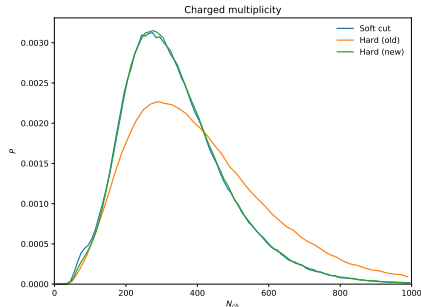
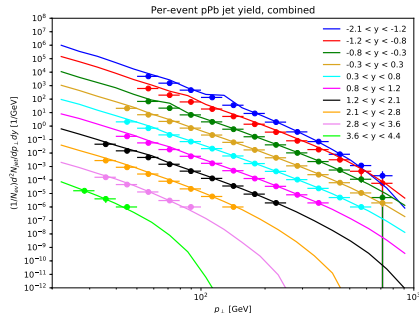


- Multiplicities well reproduced with  $\gamma p$

$(\text{Pb} \rightarrow \gamma)+\text{Pb}$ : [ATLAS: PRC 104, 014903 (2021)]

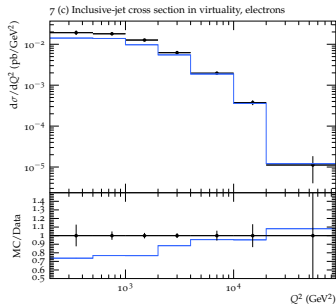


- High multiplicities missed with  $\gamma p$   
 $\Rightarrow$  Multi-nucleon interactions

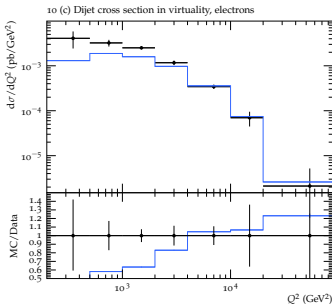


- Soft QCD: Use MC Glauber to derive impact parameters for n-n collisions
- Hard QCD: Replace smallest impact parameter n-n with a PYTHIA event  
⇒ Underlying event structures do not match
- Fixed by reweighting with impact-parameter dependent weight

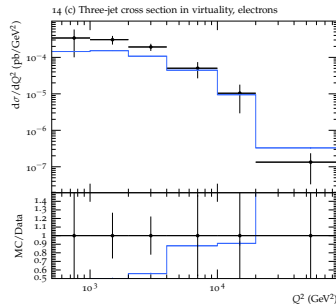
## Inclusive



## Dijet



## Trijet



- DIS events with one scattered parton in the final state + parton shower
- Okay for inclusive jets but falls below for di- and trijet
- ⇒ Need to merge hard-process events with higher parton multiplicities